

Question: Can we model long-range interactions with a single jump in molecular graphs?



Neural Atoms: Propagating Long-Range Interaction In Molecular Graphs through Efficient Communication Channel

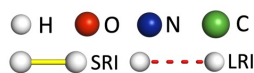
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Paper Code Slide

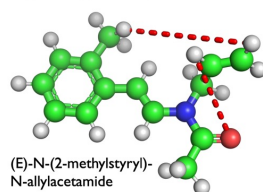
Background: Long-range Interactions

Molecular graphs consist of different types of atom interaction with different properties and functions.



- The short-range interaction (SRI) forms the structure of the molecular graph.

- The long-range interaction (LRI) could determine physical and chemical properties.

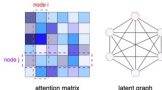


Limitations of existing approaches

Graph Neural Network

Stacking multiple GNN layers to capture LRI?

- **Over-smoothing:** representations become indistinguishable;
- **Over-squashing:** overwhelming information be squashed.



Graph Transformer

Using a fully connected graph to capture LRI?

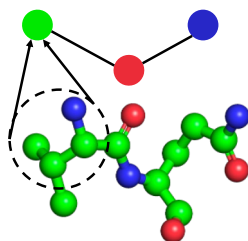
- **Irrelevant interactions:** the LRIs are naturally sparse;
- **Additional computation:** unnecessary node-pair attentions.

Motivation

Modeling distant interactions with a single jump in molecular graphs in another space.

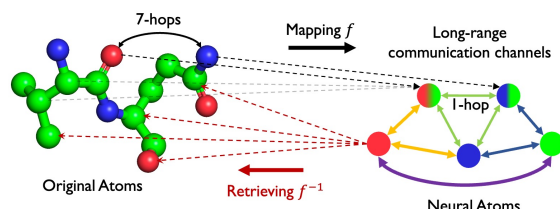
Advantages

- Learnable projection from atoms to neural atoms;
- Reducing the multi-hop long-range interaction to single-hop;
- GNN-agnostic and plug-in-and-play.



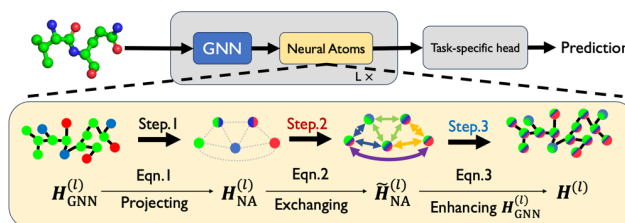
Neural Atoms

Definition 1. Neural atoms encompass a collection of virtual, parameterized atoms that symbolize a cluster of atoms within a designated molecular graph. The process entails the acquisition of knowledge that enables the transformation of conventional atoms into neural atoms, along with their interactions. This transformation can be technically executed with model-agnostic methodologies.



Learning to project all the original atoms into a few neural atoms that abstract the collective information of atomic groups in a molecule.

Implementation



Step-1. Project atom representations $H_{GNN}^{(\ell)}$ to neural atom representations $H_{NA}^{(\ell)}$.

$$H_{NA}^{(\ell)} = \text{LayerNorm} \left(Q_{NA}^{(\ell)} \oplus \text{MultiHead} \left(Q_{NA}^{(\ell)}, H_{GNN}^{(\ell)}, H_{GNN}^{(\ell)} \right) \right)$$

Step-2. Exchange information among neural atoms $H_{NA}^{(\ell)} \rightarrow \tilde{H}_{NA}^{(\ell)}$.

$$\tilde{H}_{NA}^{(\ell)} = \text{LayerNorm} \left(H_{NA}^{(\ell)} \oplus \text{MultiHead} \left(H_{NA}^{(\ell)}, H_{NA}^{(\ell)}, H_{NA}^{(\ell)} \right) \right)$$

Step-3. Project neural atoms back and enhance the atoms' representation $(H_{GNN}^{(\ell)}, \tilde{H}_{NA}^{(\ell)}) \mapsto H^{(\ell)}$.

$$H^{(\ell)} = H_{GNN}^{(\ell)} \oplus \tilde{A}_{NA}^{(\ell)} \tilde{H}_{NA}^{(\ell)}, \text{ s.t. } \tilde{A}_{NA}^{(\ell)} = \text{Aggregate} \left(\{ \hat{A}_m \}_{m=1}^M \right)^T \in \mathbb{R}^{N \times K}$$

Empirical Study

→ Neural atoms can boost the performance of various GNNs up to 27.32%.

Table 1: Test performance on three LRGB datasets. Shown is the mean \pm s.d. of 4 runs.

Model	Peptides-func		Peptides-struct		PCQM-Contact	
	AP \uparrow	MAE \downarrow	MAE \downarrow	MRR \uparrow	MRR \uparrow	MRR \uparrow
Transformer+LapPE	0.6326 \pm 0.0126	0.2529 \pm 0.0016	0.2529 \pm 0.0016	0.3174 \pm 0.0020	0.3174 \pm 0.0020	0.3174 \pm 0.0020
SAN+LapPE	0.6384 \pm 0.0121	0.2683 \pm 0.0043	0.2683 \pm 0.0043	0.3350 \pm 0.0003	0.3350 \pm 0.0003	0.3350 \pm 0.0003
GraphGPS	0.6533 \pm 0.0041	0.2500 \pm 0.0005	0.2500 \pm 0.0005	0.3337 \pm 0.0006	0.3337 \pm 0.0006	0.3337 \pm 0.0006
GCN	0.5930 \pm 0.0023	0.3496 \pm 0.0013	0.3496 \pm 0.0013	0.2329 \pm 0.0009	0.2329 \pm 0.0009	0.2329 \pm 0.0009
+ Neural Atoms	0.6228 \pm 0.0046	0.2606 \pm 0.0027	0.2606 \pm 0.0027	0.2534 \pm 0.0200	0.2534 \pm 0.0200	0.2534 \pm 0.0200
GINE	0.5498 \pm 0.0079	0.3547 \pm 0.0045	0.3547 \pm 0.0045	0.3180 \pm 0.0027	0.3180 \pm 0.0027	0.3180 \pm 0.0027
+ Neural Atoms	0.6154 \pm 0.0157	0.2553 \pm 0.0005	0.2553 \pm 0.0005	0.3126 \pm 0.0021	0.3126 \pm 0.0021	0.3126 \pm 0.0021
GCNII	0.5543 \pm 0.0078	0.3471 \pm 0.0010	0.3471 \pm 0.0010	0.3161 \pm 0.0004	0.3161 \pm 0.0004	0.3161 \pm 0.0004
+ Neural Atoms	0.5996 \pm 0.0033	0.2563 \pm 0.0020	0.2563 \pm 0.0020	0.3049 \pm 0.0006	0.3049 \pm 0.0006	0.3049 \pm 0.0006
GatedGCN	0.5864 \pm 0.0077	0.3420 \pm 0.0013	0.3420 \pm 0.0013	0.3218 \pm 0.0011	0.3218 \pm 0.0011	0.3218 \pm 0.0011
+ Neural Atoms	0.6562 \pm 0.0075	0.2385 \pm 0.0017	0.2385 \pm 0.0017	0.3258 \pm 0.0003	0.3258 \pm 0.0003	0.3258 \pm 0.0003
GatedGCN+RWSE	0.6069 \pm 0.0035	0.3357 \pm 0.0006	0.3357 \pm 0.0006	0.3242 \pm 0.0008	0.3242 \pm 0.0008	0.3242 \pm 0.0008
+ Neural Atoms	0.6591 \pm 0.0050	0.2568 \pm 0.0005	0.2568 \pm 0.0005	0.3262 \pm 0.0010	0.3262 \pm 0.0010	0.3262 \pm 0.0010

→ Neural atoms without 3D information and half the #params. achieve competitiveness or outperform the Ewald-based approach (previous SOTA).

Table 2: Validation energy MAE and MSE comparison on OE62 dataset.

Model	Energy MAE \downarrow		Energy MSE \downarrow		Number of Params.	
	MAE	MSE	MAE	MSE	Params	Params
SchNet (Schütt et al., 2017)	0.1351	0.0658	0.1351	0.0658	2.75 M	2.75 M
+ Ewald Block	0.0811	0.0301	0.0811	0.0301	12.21 M	12.21 M
+ Neural Atoms	0.0834	0.0309	0.0834	0.0309	2.63 M	2.63 M
PaiNN (Schütt et al., 2021)	0.6049	0.0133	0.6049	0.0133	12.52 M	12.52 M
+ Ewald Block	0.0590	0.0134	0.0590	0.0134	15.68 M	15.68 M
+ Neural Atoms	0.0558	0.0122	0.0558	0.0122	6.05 M	6.05 M
DimeNet++ (Gasteiger et al., 2020)	0.0501	0.0117	0.0501	0.0117	2.76 M	2.76 M
+ Ewald Block	0.0479	0.0107	0.0479	0.0107	4.75 M	4.75 M
+ Neural Atoms	0.0551	0.0129	0.0551	0.0129	1.97 M	1.97 M

→ Neural Atoms are better than multiple fully connected Virtual Nodes.

Table 14: Performance for virtual nodes (VNs) and neural atoms (NAs) in Peptide-Func, evaluated by AP (the higher, the better).

Model	Method	#VNs/#NAs = 5		#VNs/#NAs = 15		#VNs/#NAs = 75		#VNs/#NAs = 135	
		AP	MAE	AP	MAE	AP	MAE	AP	MAE
GCN	VNs	0.5566	0.5543	0.5566	0.5588	0.5566	0.5588	0.5566	0.5588
	NAs	0.5962	0.5859	0.5903	0.6220	0.5903	0.6220	0.5903	0.6220
GINE	VNs	0.5437	0.5500	0.5426	0.5426	0.5426	0.5426	0.5426	0.5426
	NAs	0.6107	0.6128	0.6147	0.6154	0.6147	0.6154	0.6147	0.6154
GCNII	VNs	0.5086	0.5106	0.5077	0.5083	0.5077	0.5083	0.5077	0.5083
	NAs	0.6061	0.5862	0.5909	0.5996	0.5909	0.5996	0.5909	0.5996
GatedGCN	VNs	0.5810	0.5868	0.5761	0.5810	0.5761	0.5810	0.5761	0.5810
	NAs	0.6660	0.6533	0.6562	0.6562	0.6562	0.6562	0.6562	0.6562

→ Neural Atoms have sparse attention and establish inter-communications.

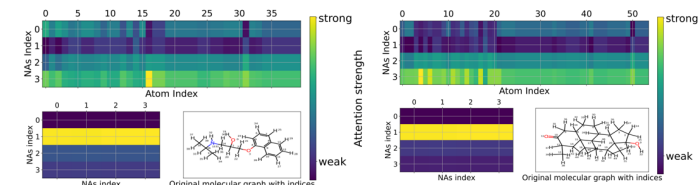


Figure 17: Mutagenicity test set index-18

Figure 19: Mutagenicity test set index-29